

# LUKAS NABERGALL

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## EDUCATION

### **Ph.D. in Combinatorics and Optimization** September 2017 — December 2022

University of Waterloo, Waterloo, ON

Advisor: Dr. Karen Yeats

Thesis: *Enumerative perspectives on chord diagrams*

Relevant Coursework: Deep Learning in Computational Discrete Optimization, Combinatorial Optimization, Graph Theory, Analytic Number Theory, Algebraic Enumeration, Feynman Diagrams, Public-Key Cryptography, Matroid Theory, Combinatorial Hopf Algebras

### **B.A./M.A. in Mathematics** August 2013 — August 2017

University of South Florida, Tampa, FL

Advisors: Dr. Nataša Jonoska and Dr. Masahico Saito

Thesis: *Patterns in Words Related to DNA Rearrangements*

Relevant Coursework: Independent Study in Machine Learning, Materials Physics, Algebraic Automata Theory, Advanced Linear Algebra, Symbolic Computations, Statistics, Partial Differential Equations, Differential Geometry, Topology, Independent Study in General Relativity, Graph Theory, Abstract Integration, Applied Complex Analysis, Real Analysis

## EXPERIENCE

### **Graduate Research Assistant** September 2017 — August 2022

*University of Waterloo*

*Advisor: Dr. Karen Yeats*

- Studied the exact enumeration of restricted hereditary classes of chord diagrams.
- Constructed structural decompositions for chord diagrams to solve certain Dyson-Schwinger equations from quantum field theory.

### **Teaching Assistant** September 2017 — August 2022

*University of Waterloo*

*Department of Combinatorics and Optimization*

- Conducted tutorials, graded assignments, and proctored exams for MATH 115 Linear Algebra, MATH 239 Introduction to Combinatorics, CO 630 Algebraic Enumeration, and CO 370 Deterministic Operations Research Models.

### **Graduate Research Assistant** August 2016 — August 2017

*University of South Florida, USF Math/Bio Lab*

*PI: Dr. Nataša Jonoska and Dr. Masahico Saito*

- Using topological and graph-theoretic methods, investigated the connectivity of words under certain string operations.

**Graduate Instructional Assistant**

August 2016 — May 2017

*University of South Florida**Department of Mathematics and Statistics*

- Graded assignments and proctored tests for MAC 2281 Engineering Calculus I and MAS 3105 Linear Algebra.

**Undergraduate Research Assistant**

May 2015 — August 2016

*University of South Florida, USF Math/Bio Lab**PI: Dr. Nataša Jonoska and Dr. Masahico Saito*

- Investigated generalized patterns in words and explored the properties of indices and distances on words defined via pattern removal operations.
- Applied these patterns, indices, and distances to the study of highly complex genome rearrangements in the ciliate *Oxytricha trifallax*.

**Undergraduate Researcher**

October 2013 — January 2015

*University of South Florida**Advisor: Dr. Stephen Suen*

- Produced some weak improvements to the best known inequalities approaching Vizing's conjecture on the domination number of the Cartesian product of graphs.
- Examined the domination number of the Cartesian product of Erdős-Rényi random graphs.

**Student Researcher**

June 2012 — August 2012

*Camp Euclid**Advisor: Dr. David Gay*

- Investigated Goldbach's conjecture, Pascal's triangle, and a polygon unfolding problem.
- Collaborated with other students from around the world.

PUBLICATIONS

A. A. Mahmoud, L. Nabergall, *Pattern avoidance and connectivity in chord diagrams*, in submission.

P.-H. Balduf, A. Cantwell, K. Ebrahimi-Fard, L. Nabergall, N. Olson-Harris, K. Yeats, *Tubings, chord diagrams, and Dyson-Schwinger equations*, accepted into J. London Math. Soc.

L. Nabergall, *The combinatorics of a tree-like functional equation for connected chord diagrams*, *Combinatorial Theory*, **3**:3 (2023), doi:10.5070/C63362791.

D. A. Cruz, M. M. Ferrari, N. Jonoska, L. Nabergall, M. Saito, *Insertions Yielding Equivalent Double Occurrence Words*, *Fundamenta Informaticae*, **171**:1–4 (2020) 113–132, doi:10.3233/FI-2020-1875.

L. Nabergall, J. Toth, L. Cousins, *Training Hard-Threshold Networks with Combinatorial Search in a Discrete Target Propagation Setting*, previously submitted to International Conference on Learning Representations.

L. Nabergall, A. Navas, E. Winsberg, *An antidote for hawkmoths: On the prevalence of structural chaos in non-linear modeling*, *European Journal for Philosophy of Science*, **9**:21 (2019), arXiv:1706.07528.

J. Braun, L. Nabergall, R. Neme, L. Landweber, M. Saito, N. Jonoska, *Russian Doll Genes and Complex Chromosome Rearrangements in *Oxytricha trifallax**, *G3: Genes, Genomes, Genetics*, **8**:5 (2018) 1669–1674, doi:10.1534/g3.118.200176.

N. Jonoska, L. Nabergall, M. Saito, *Patterns and Distances in Words Related to DNA Rearrangement*, *Fundamenta Informaticae*, **154** (2017) 225–238, doi:10.3233/FI-2017-1563.

## PROJECTS

### **8-bit Breadboard Computer**

- ~500 Hz, 16 byte RAM; modified version of Ben Eater’s design.
- Constructed to gain further familiarity with electronics and computer hardware design.

### **CollaboRatings - CDP Climate Hackathon 2020 Winner**

- Constructed and visualized a KPI model for cross-sector collaboration on climate mitigation strategies between US cities and corporations.
- Analyzed free-form responses in CDP surveys using spaCy text embeddings to automatically identify potential agreement on climate issues.
- Competed as Team Rocket with Savannah Wu, Alejandro Navas, and Cynthia Wang.

### **Terrace: PyTorch Utilities Library**

[github.com/lnabergall/terrace](https://github.com/lnabergall/terrace)

- A framework built on top of PyTorch that adds customizable data input and processing pipelines, training, evaluation, and monitoring tools, and a variety of standard machine learning components, including evaluation metrics, hyperparameter containers, regularizers, and more.
- Supports a variety of machine learning paradigms, including supervised, unsupervised, and reinforcement learning.
- Open-sourced.

### **MultiLM**

[github.com/lnabergall/multi-lm](https://github.com/lnabergall/multi-lm)

- Trained and evaluated multilingual and, eventually, multi-domain language models using a simple modification to standard neural language models.
- Observed significant transfer learning and a small increase in perplexity as the number of languages increases.

**Li-Fi Transmitter and Receiver**

- Designed and constructed a prototype Li-Fi transmitter and receiver capable of communicating high-bandwidth audio over a significant distance.
- See this [YouTube video](#) for a demonstration of the system, completed collaboratively with Mark Steele, Nathan Hayford, Carlton Drew, Nikki Hudson, and Zhimin Shi, students and professors at the University of South Florida.

**WordExplorer**

[github.com/lnabergall/word-explorer](https://github.com/lnabergall/word-explorer)

- A library that implements a variety of tools for working with words, patterns, pattern indices, and pattern-based word distances.
- Based on a series of papers co-authored with Nataša Jonoska, Masahico Saito, Jasper Braun, and others.

**Knowledge Database**

[github.com/lnabergall/knowledge-database](https://github.com/lnabergall/knowledge-database)

- The backend for an open, editable, structured knowledge store (i.e. a wiki variant).
- Includes a robust voting system for managing edits, mechanisms to encourage user transparency, and shorter, more structured articles (or content pieces) than Wikipedia, making it better suited for the accumulation and distribution of advanced research-oriented subject knowledge.

INVITED TALKS

<i>Finding structure in chord diagrams</i> ICE-TCS Research Seminar Reykjavik University, Iceland	November 24, 2022
<i>The enumerative universe of chord diagrams</i> Ontario Combinatorics Workshop University of Waterloo, Ontario	May 13, 2022
<i>Enumerating hereditary classes of chord diagrams</i> Algebraic and Enumerative Combinatorics Seminar University of Waterloo, Ontario	June 10, 2021
<i>Weighted generating functions for weighted chord diagrams</i> Algebraic and Enumerative Combinatorics Seminar University of Waterloo, Ontario	June 4, 2020
<i>Connectivity and terminal chords in chord diagrams</i> CMS Winter Meeting Toronto, Ontario	December 9, 2019
<i>Patterns in Words Related to DNA Rearrangements</i> Master's Thesis Defense University of South Florida, Tampa, Florida	March 10, 2017

*Complex Rearrangements in the  
Highly Scrambled Genome of *O. trifallax** June 15, 2016  
The Allied Genetics Conference  
Orlando, Florida

*Recurring Patterns in a Highly Scrambled Ciliate Genome* April 6, 2016  
USF Research and Arts Colloquium  
University of South Florida, Tampa, Florida

*Patterns and Distances for Double Occurrence Words* March 4, 2016  
USF Math Club  
University of South Florida, Tampa, Florida

*Patterns and Distances for Double Occurrence Words* February 27, 2016  
MAA-FTYCMA Joint Conferences  
Saint Leo University, Saint Leo, Florida

#### SKILLS

Programming: Python, C++, Java, L<sup>A</sup>T<sub>E</sub>X, HTML, CSS  
Languages: English, Danish